

# Statistical Machine Learning

## Ensemble Learning

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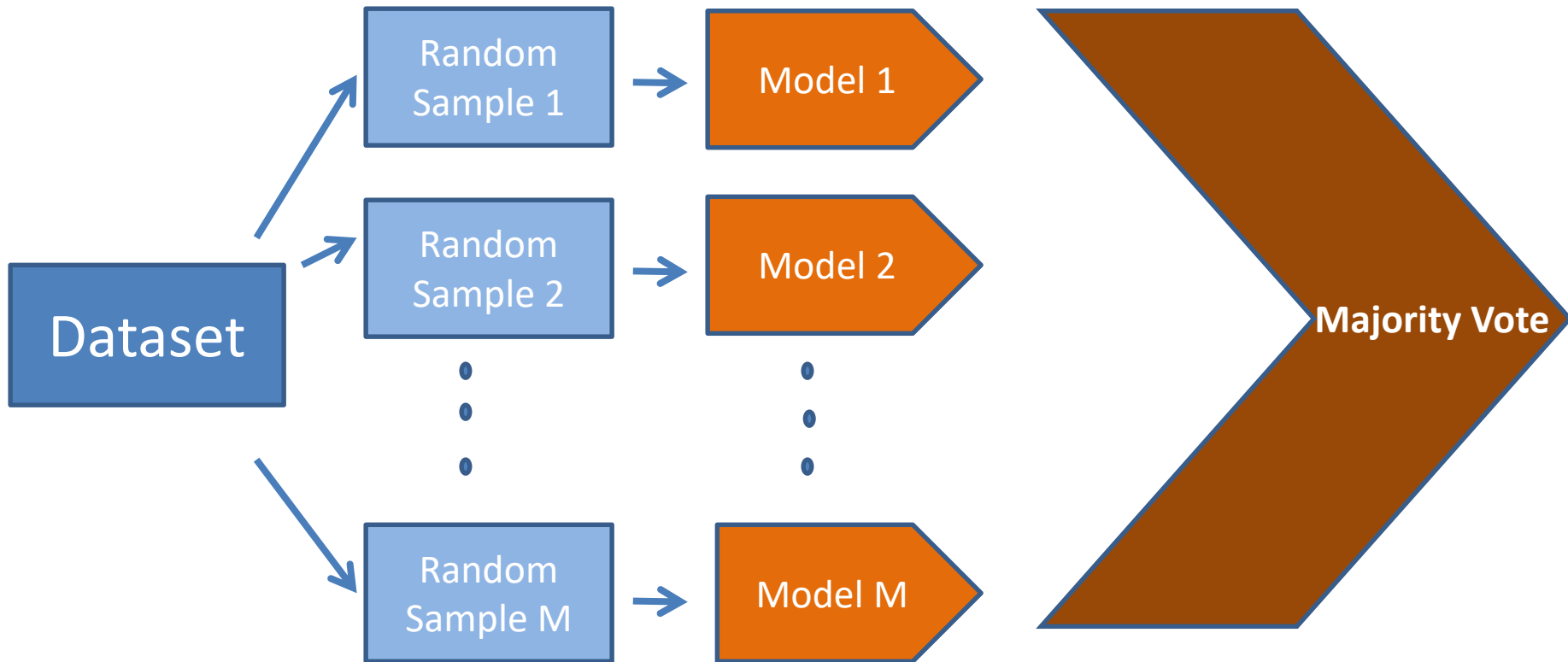
**Idea:** train several (many) predictive models and combine the results to make a final predictive model.

A few popular methods:

- Bagging
- Boosting
- Stacking
- Random Forests

# Bagging

Bootstrap **A**ggregation:



# Bagging

Choose a type of model (e.g. neural net)

1. Obtain a random sample (with replacement) from the training dataset, both of size  $n$
2. Train a model using the random sample

Repeat steps 1-2  $M$  times.

Majority vote/average of the predictions from  $M$  models for the final prediction model.

# Example: Bank Notes



# Training and Test sets

```
> str(ss)
```

```
'data.frame': 1235 obs. of 6 variables:  
 $ variance: num 4.546 3.866 3.457 0.329 3.591 ...  
 $ skewness: num 8.17 -2.64 9.52 -4.46 3.01 ...  
 $ kurtosis: num -2.459 1.924 -4.011 4.572 0.729 ...  
 $ entropy : num -1.462 0.106 -3.594 -0.989 0.564 ...  
 $ type :int 0 0 0 0 0 0 0 0 0 ...  
 $ genuine : Factor w/ 2 levels "no","yes": 1 1 1 1 1 1 1 1 1 1 ...
```

```
> str(tt)
```

```
'data.frame': 137 obs. of 6 variables:  
 $ variance: num 3.0948 3.0864 3.8999 -1.2424 -0.00129 ...  
 $ skewness: num 8.732 -2.584 1.734 -1.718 0.139 ...  
 $ kurtosis: num -2.901 2.231 1.601 -0.526 -0.197 ...  
 $ entropy : num -0.96682 0.30947 0.96765 -0.21036 0.00818 ...  
 $ type :int 0 0 0 1 1 1 1 1 1 0 ...  
 $ genuine : Factor w/ 2 levels "no","yes": 1 1 1 2 2 2 2 2 2 1 ...
```

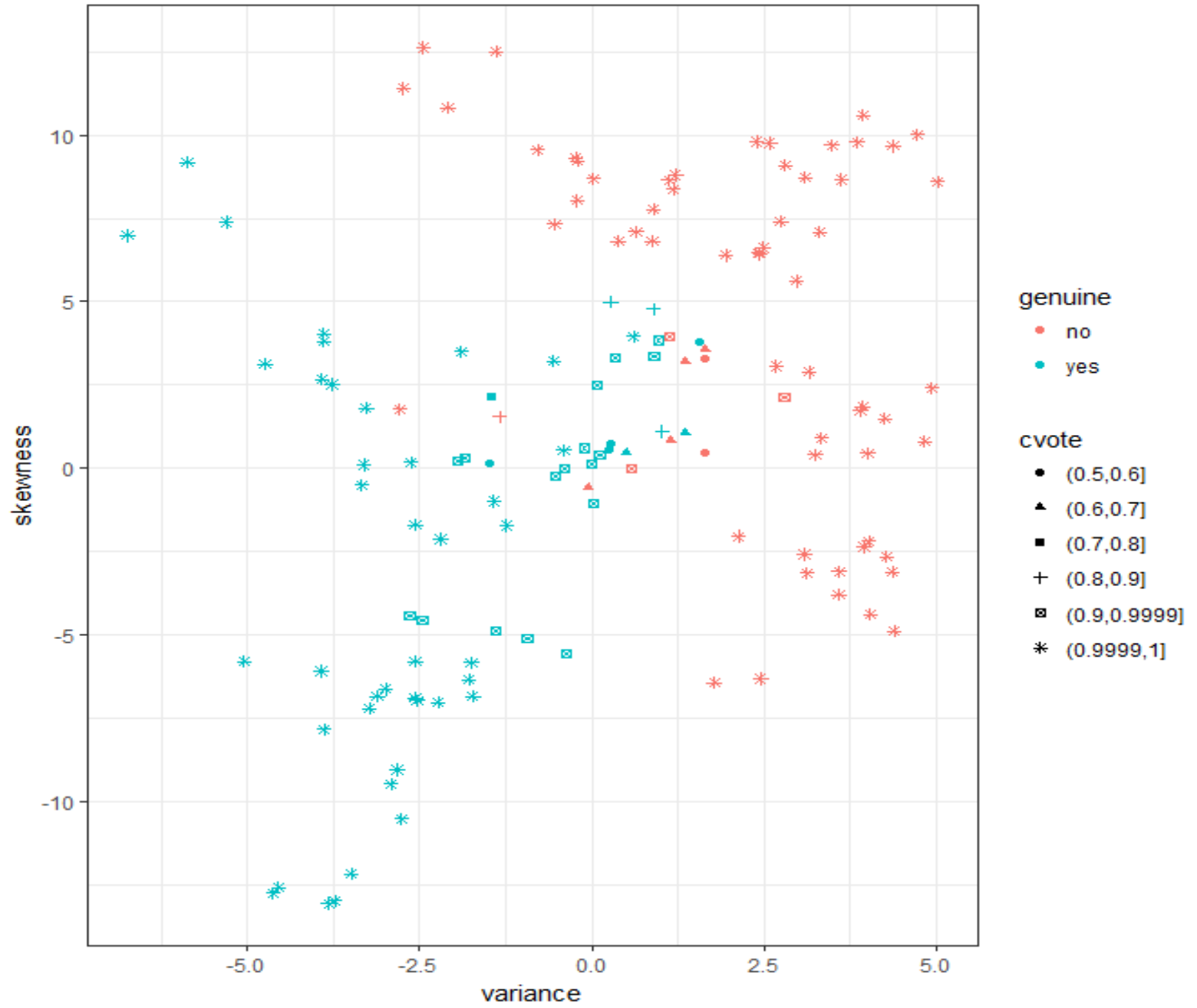
# Bagging kNN in R: bnn

```
> library(FNN)
> out <- ownn(ss[,1:2], tt[1:2], cl=ss[,6], testcl=tt[,6])
> out$accuracy
```

knn	ownn	bnn
0.9343066	0.9343066	0.9416058

*Number of neighbors  $k$  is chosen by 5-fold CV*

# Results of Majority Voting





# Bias-Variance Tradeoff & Bagging

Bagging is

- probably worthwhile when a method tends to produce highly variable model fits across different training sets (i.e., high variance).
- probably not worthwhile for low variance methods

# Bagging vs. Boosting

M random samples are drawn from original dataset

M models fit separately

Each model's vote is equally important, i.e. equally weighted.

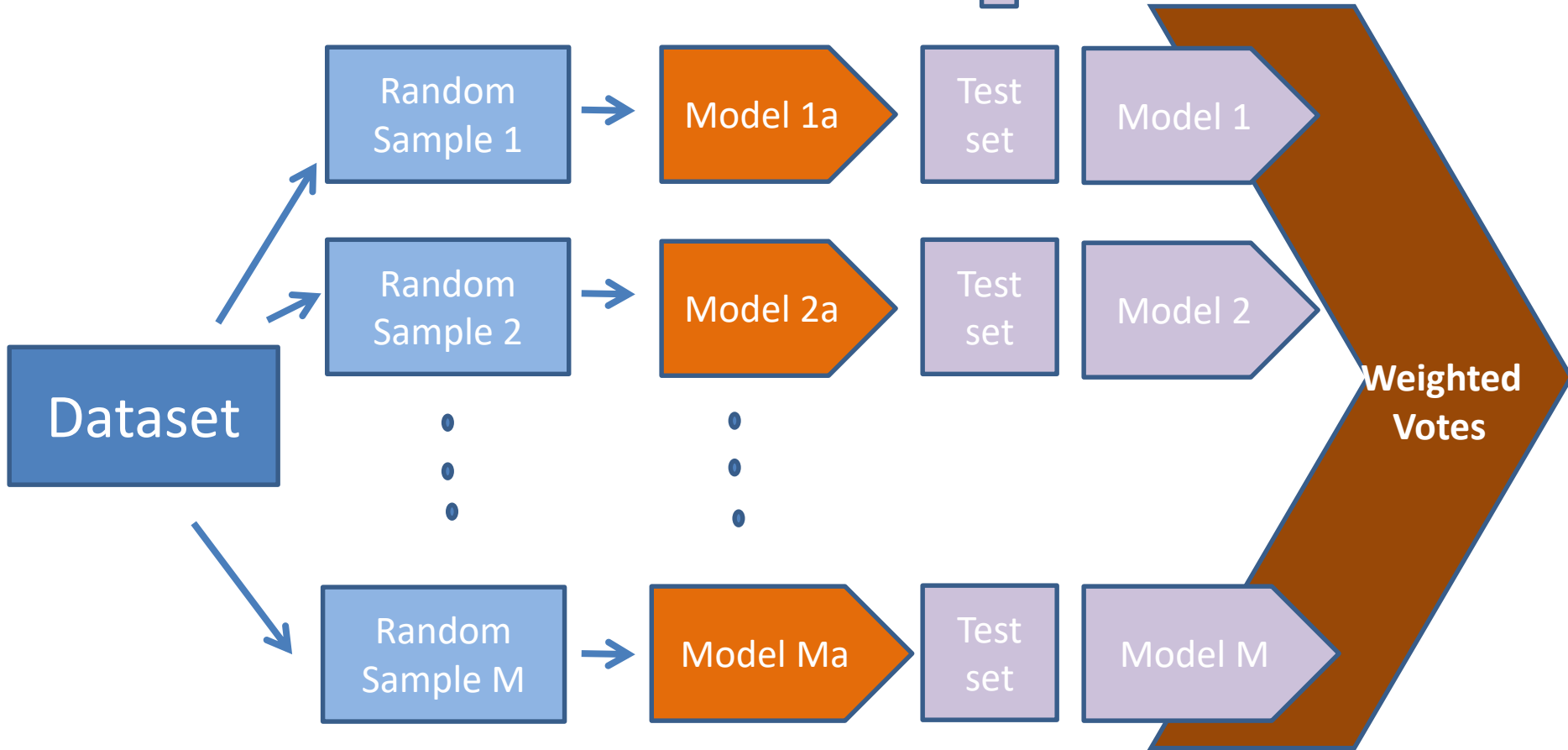
**Initialize:** Bagging

**Iterate:** Draw M random samples, but give points that were misclassified in the previous round more weight (more likely to be in the samples). Fit M models

Each model's vote is weighted by its accuracy to build the final prediction model.

# Boosting

Give more weight to misclassified points



# Boosting

- Might reduce both bias and variance

OR

- Might be misled by a few outliers

# Stacking

- Combines different methods of training a model
- Uses the predictions of the models as inputs to a machine learning algorithm to make the final prediction

# Stacking

