# Math 243 

Day 3
Traffic Fatalities - Inv. A
Random Babies - Inv. B

## Last Time - Did traffic fatalities decrease after the Federal Speed Limit Law?

- we found the percent change in fatalities dropped by $17.14 \%$ after the law was passed.


Is $17.14 \%$ a large change compared to the changes between other years?

## How large is "large"?

When deciding whether particular value is extreme or not, it is helpful to consider the distribution of all values of the variable.

In particular, consider the center, spread and shape of the distribution.

## Describing center, spread and shape of a distribution

## Numerical summaries of center:

Mean (average) or Median (middle value) give us an idea of a "typical value" of the variable.

Numerical summary of spread:
Standard deviation gives us an idea of a "typical deviation" from the mean of the variable, i.e. how much variation there is.

Words to describe shape:

- Symmetric, skewed right or skewed left
- Bell shaped (one hill), bimodal (two hills) , uniform (rectangle)....


## Visualizing Center, Shape and Spread


3. Describe the center, shape and spread of a distribution, from a

## Traffic Fatalities - Inv. A

Along with me (or at home), try parts i), j), k), and I).

Part $m$ ) is on the first homework assignment.

# Describing the distribution of percent changes in traffic fatalities 

| Mean: $\square$ Guess $\square$ Actual |  |
| :--- | :---: |
| Median: $\square$ Guess $\square$ Actual |  |
| Std dev. $\square$ Guess $\square$ Actual |  |
| IQR: $\square$ Guess $\square$ Actual |  |
|  | Delete |

Most percent changes were clustered around $6 \%$ with a typical deviation from $6 \%$ of about $16 \%$. There are a few extremely large percent changes.


## Is a change of $-17.14 \%$ unusual?

Most percent changes were clustered around $6 \%$ with a typical deviation from $6 \%$ of about 16\%. There are a few extremely large percent changes.

Typically changes were between
6-16=-10\% and
6+16=24\%
so a change of $-17.14 \%$ was unusual.


## A "big" idea

If the shape of the distribution is roughly bell-shaped, then the mean and standard deviation (SD) can be used to determine whether a value is "unusual" or not.

A general rule of thumb is that observations that are more than $\mathbf{2 S D}$ from the mean are "unusual" ...

$$
\text { Atypical < Mean + } 2 \text { SD < typical < Mean - } 2 \text { SD < Atypical }
$$

4. Determine whether a particular observation is unusual compared to a distribution

## A "big" idea

If the shape of the distribution is roughly bell-shaped, then the mean and standard deviation (SD) can be used to determine whether a value is "unusual" or not.

A general rule of thumb is that observations that are more than $\mathbf{2 S D}$ from the mean are "unusual"...

Atypical < Mean + 2 SD < typical < Mean - 2 SD < Atypical
...but this rule only works well if the distribution is roughly bell-shaped

## Learning Objectives again - Inv. A, Day 2 (and Day 3)

1. State the five steps of using data to answer a question
2. Calculate the mean, median, and standard deviation of a dataset, by hand or with an applet.
3. Describe the center, shape and spread of a distribution, from a dotplot or histogram
4. Determine whether a particular observation is unusual compared to a distribution

## Learning Objectives - Inv. B, Day 3

1. Define the term "probability"
2. Estimate a probability by simulating a random process
purple $=$ a statistical term whose definition you should memorize (use the glossary!)

## Random Babies - Inv. B

Suppose 4 babies are randomly returned to their mothers.

What is the probability that at least one mother will receive the correct baby?

This investigation will introduce you to the idea of simulating a random process. We'll start today and finish on Friday.

## Random Babies - Inv. B

- Do at least parts a, b, and d now. Report your results from part d to Dr. O. Continue working on parts e, $f$ and $g$.

| Number of matches | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Count |  |  |  |  |  |
| Proportion |  |  |  |  |  |

- Try the applet for part j at home before class on Friday.

2. Estimate a probability by simulating a random process

## What is meant by "Probability"?

Notice that we estimated the probability of at least one mother receiving the correct baby by repeatedly

- "shuffling" the babies,
- dealing babies out to mothers, and
- counting the number of times each mother received the correct baby.

The definition of "probability" we'll use in this class is the long run relative frequency of times an event occurs

1. Define the term "probability"
