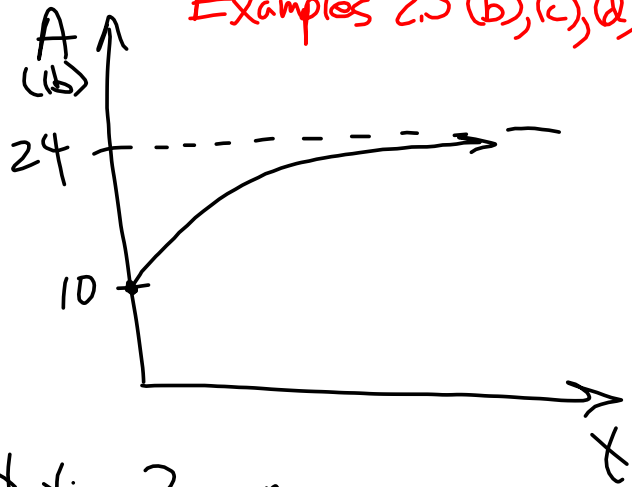


Examples 2.5 (b), (c), (d)



Looking for  $A = t$  or  $A = A(t)$  Concentration?

In:  $7 \frac{\text{gal}}{\text{min}} \cdot 0.3 \frac{\text{lb}}{\text{gal}} = 2.1 \frac{\text{lb}}{\text{min}}$

Out:  $7 \frac{\text{gal}}{\text{min}} \cdot \frac{A}{80} \frac{\text{lb}}{\text{gal}} = \frac{7A}{80} \frac{\text{lb}}{\text{min}}$

Total  $\frac{dA}{dt}$

$\frac{A}{80} \frac{\text{lbs}}{\text{gal}}$

$\frac{dA}{dt} = \frac{dA}{dt}_{\text{in}} - \frac{dA}{dt}_{\text{out}}$

$\frac{dA}{dt} = 2.1 - \frac{7A}{80}$

$A(0) = 10$

Solve  $\frac{dy}{dx} - 3y = 2$

~~$\int x^2 \frac{1}{dx}$~~

$$\frac{dy}{dx} = 3y + 2$$

$$dy = (3y + 2) dx$$

$$\frac{dy}{3y + 2} = dx$$

$$\int \frac{dy}{3y + 2} = \int dx$$

$$\frac{1}{3} \ln|3y + 2| = x + C_2$$

Solve for y

$|x| = 5$

$x = \pm 5$

$$\ln|3y + 2| = 3x + C_3$$

$$e^{\ln|3y + 2|} = e^{3x + C_3}$$

$$|3y + 2| = e^{3x} e^{C_3}$$

$$3y + 2 = \pm C_4 e^{3x}$$

↓  
in there!

$$3y + 2 = C_5 e^{3x}$$

$$3y = C_5 e^{3x} - 2$$

$$y = C_6 e^{3x} - \frac{2}{3}$$

$x^7 x^{12} =$

$x^a x^b = x^{a+b}$

$$\frac{dA}{dt} = 2.1 - \frac{7}{80}A, \quad A(0) = 10$$

Solution

$$A = 24 - 14e^{-\frac{80}{7}t}$$

$$dA = \left(2.1 - \frac{7}{80}A\right) dt$$

$$\frac{dA}{2.1 - \frac{7}{80}A} = dt$$

$$-\frac{7}{80} \ln \left| 2.1 - \frac{7}{80}A \right| = t + C$$

$$\ln \left( 2.1 - \frac{7}{80}A \right) = -\frac{80}{7}t + C$$

$$2.1 - \frac{7}{80}A = e^{-\frac{80}{7}t + C}$$

$$2.1 - \frac{7}{80}A = C e^{-\frac{80}{7}t}$$

$$-\frac{7}{80}A = C e^{-\frac{80}{7}t} - 2.1$$

$$A(0) = 10$$

$$A = C e^{-\frac{80}{7}t} + 24$$

$$\rightarrow 10 = C + 24$$

$$-14 = C$$

$$A = 24 - 14e^{-\frac{80}{7}t}$$