

$$y' + 3y = 4, \quad y(0) = 1 \quad y = \frac{4}{3} + Ce^{-3t}$$

$$y' + 3y = 0$$

$$y' = -3y$$

$$y = Ce^{-3t}$$

$$y_p = C$$

$$y_p' = 0$$

$$3C = 4$$

$$C = \frac{4}{3}$$

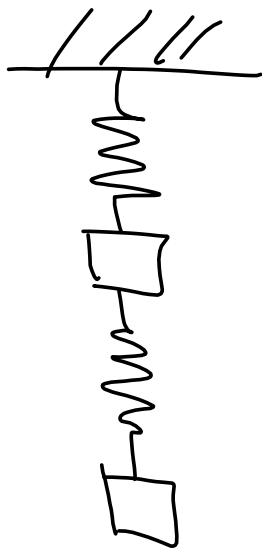
$$y'' + 5y' + 7y = 4e^{-3t}, \quad y(0) = \quad y'(0) =$$

underdamped $b^2 - 4ac < 0$

$$y = e^{-\frac{5}{2}t} (C_1 \sin \frac{\sqrt{3}}{2}t + C_2 \cos \frac{\sqrt{3}}{2}t) + Ae^{-3t}$$

$$y'' + 10y' + 2y = \text{ } \quad y = C_1 e^{-2t} + C_2 e^{-2t}$$

overdamped
 $b^2 - 4ac > 0$



$$e^x = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \dots$$

$$y = a_0 + a_1x + a_2x^2 + a_3x^3 + \dots$$

$$y' + 3y = \dots$$

$$\sin x = x - \frac{1}{6}x^3 + \frac{1}{120}x^5 - \dots$$

$$y' = a_1 + 2a_2x + 3a_3x^2 + \dots$$

