

1. Find the derivative of each function without using your calculator. You *MAY* use the course formula sheet. Give your answers using correct derivative notation.

(a) $y = 2 \sin 3x$

(b) $y = 4e^{-0.5t}$

(c) $x = t^2 + 5t - 4$

(d) $y = 3.4 \cos(1.3t - 0.9)$

(e) $y = te^{-3t}$

(f) $x = 4e^{-2t} \sin(3t + 5)$

2. Find the second derivatives of the functions from parts (a)-(c) of Exercise 1. Give your answers using correct derivative notation.

3. The height y of a mass on a spring, from its equilibrium point, is measured in inches. Time t is in seconds, and we are given that

$$\left. \frac{dy}{dt} \right|_{t=3} = 1.87$$

- (a) What are the units of the number 3? What quantity does t measure?
- (b) What are the units of the number 1.87? What physical quantity is it representing?
- (c) Write a sentence summarizing the given mathematical statement. *DO NOT* use the word *derivative*, *DO* use one of the words *upward* or *downward*.

4. The temperature T , in degrees Fahrenheit, of a burrito when it comes out of a microwave oven is 134° F. It's too hot to eat, so you let it cool for a bit. Suppose that time t is measured in minutes and we have

$$\left. \frac{dT}{dt} \right|_{t=5} = -2.3$$

Write a sentence summarizing what this tells us. Include (correct!) units with any numbers. *DO NOT* use the words *derivative*, *negative*, or the negative sign. *DO* use one of the words *increasing* or *decreasing*.

5. The temperature T , in degrees Fahrenheit, of a burrito when it comes out of a microwave oven is 134° F. It's too hot to eat, so you let it cool for a bit in a 68° F room. You start playing a video game and forget about the burrito until several hours later. Sketch a graph of the temperature of the burrito as a function of time. Label two numerical values on the vertical (T) axis.