For each system given, do each of the following.

- (a) Use Wolfram Alpha to find the eigenvalues and eigenvectors.
- (b) Draw the phase portrait using only the eigenvalues and eigenvectors. Then check your answer with the online phase plane plotter.
- (c) Tell whether the origin is a nodal sink or source, spiral sink or source, saddle point or center. If it is a nodal sink or source, tell whether the node is proper, improper or neither.
- (d) Tell whether the origin is unstable, asymptotically stable, or neutrally stable.

1. 
$$\mathbf{x}' = \begin{bmatrix} 5 & -1 \\ 3 & 1 \end{bmatrix} \mathbf{x}$$
  
2.  $\mathbf{x}' = \begin{bmatrix} 2 & -1 \\ 3 & -2 \end{bmatrix} \mathbf{x}$   
3.  $\mathbf{x}' = \begin{bmatrix} 1 & -4 \\ 4 & -7 \end{bmatrix} \mathbf{x}$   
4.  $\mathbf{x}' = \begin{bmatrix} 1 & -5 \\ 1 & -3 \end{bmatrix} \mathbf{x}$   
5.  $\mathbf{x}' = \begin{bmatrix} 2 & -5 \\ 1 & -2 \end{bmatrix} \mathbf{x}$   
6.  $\mathbf{x}' = \begin{bmatrix} 3 & -2 \\ 4 & -1 \end{bmatrix} \mathbf{x}$ 

## Math 322 ASSIGNMENT 17, SPRING 2013 Due at 3 PM Monday May 13th

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