

$$\frac{8}{2} = 4 \text{ because } 2 \cdot 4 = 8$$

$$\frac{a}{b} = c \quad c \cdot b = a$$

$$\frac{0}{5} = 0 \text{ because } 5 \cdot 0 = 0$$

$$\frac{7}{0} = a \iff 0 \cdot a = 7 \text{ no solution}$$

$\frac{7}{0}$ DNF

$$\frac{0}{0} = a \iff 0 \cdot a = 0 \text{ true for all } a$$

$\frac{0}{0}$ is undefined

$$X' = \begin{bmatrix} -\frac{3}{2} & -\frac{1}{4} \\ -1 & -\frac{3}{2} \end{bmatrix} X$$

A

$$\begin{bmatrix} x_1' \\ x_2' \end{bmatrix} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$\lambda = -2, -1$$

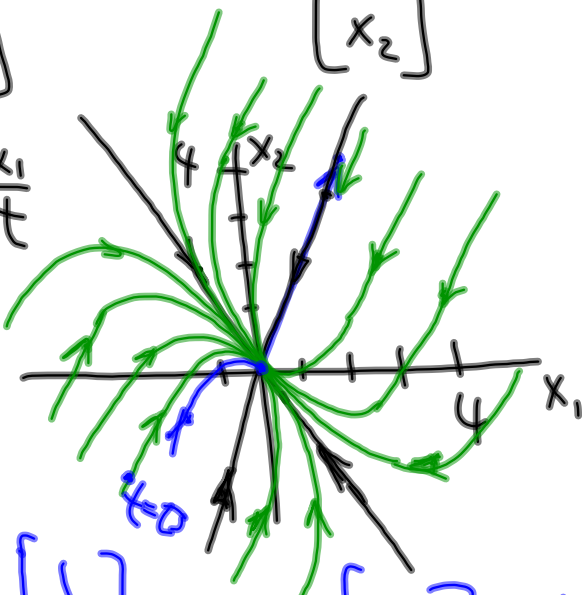
λ_1, λ_2

$$\vec{k} = \begin{bmatrix} 1 \\ 2 \end{bmatrix}, \begin{bmatrix} -1 \\ 2 \end{bmatrix}$$

\vec{k}_1, \vec{k}_2

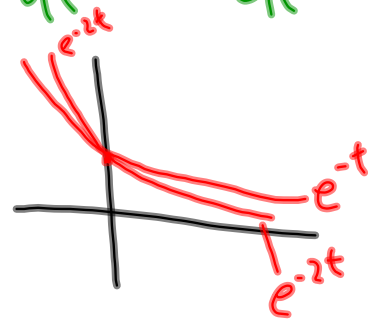
$$A(c\vec{k}_i) = \lambda_i c\vec{k}_i$$

$$x_i' = \frac{dx_i}{dt}$$



At some time,
 $x_1 = 2, x_2 = 4$ and
 $\frac{dx_1}{dt} = -4, \frac{dx_2}{dt} = -8$

$$\vec{X} = c_1 \begin{bmatrix} 1 \\ 2 \end{bmatrix} e^{-2t} + c_2 \begin{bmatrix} -1 \\ 2 \end{bmatrix} e^{-t}$$



As we go backward in time, t is neg,
 so first term is dominant. Going forward,
 $e^{-t} > e^{-2t}$, so second term is dominant.

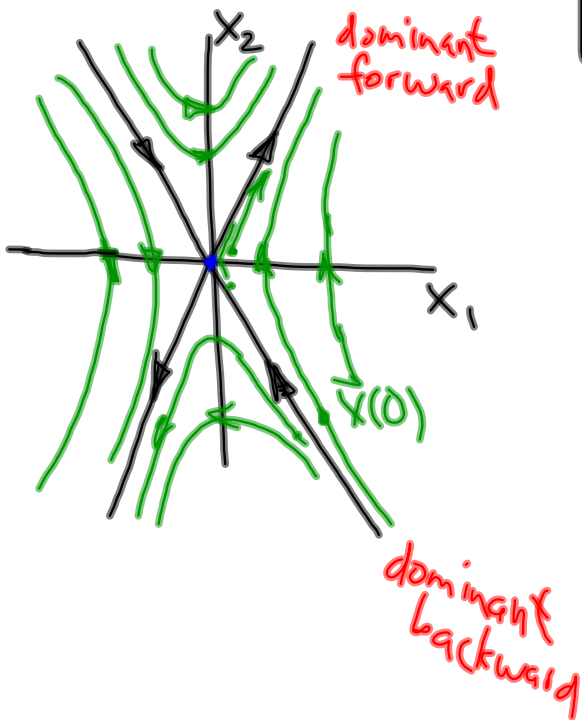
$$\vec{x}' = \begin{bmatrix} 1 & 1 \\ 4 & 1 \end{bmatrix} \vec{x}$$

$$\lambda = 3, -1$$

$$\vec{k} = \begin{bmatrix} 1 \\ 2 \end{bmatrix}, \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 2 \end{bmatrix} e^{3t}$$

$$\begin{bmatrix} 1 \\ -2 \end{bmatrix} e^{-t}$$

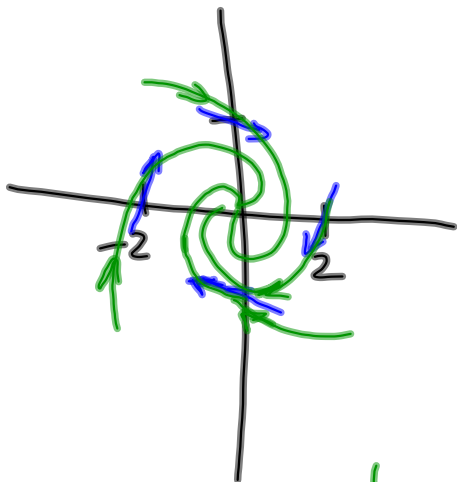


$$\vec{X}' = \begin{bmatrix} -\frac{1}{2} & 1 \\ -1 & -\frac{1}{2} \end{bmatrix} \vec{X} \quad \lambda = -\frac{1}{2} \pm i \quad \vec{k} = \begin{bmatrix} 1 \\ \pm i \end{bmatrix}$$

$$e^{\lambda t} = e^{-\frac{1}{2}t} (\cos t + i \sin t)$$

$$\vec{X} = \begin{bmatrix} c_1 \cos t + c_2 \sin t \\ d_1 \cos t + d_2 \sin t \end{bmatrix} e^{-\frac{1}{2}t}$$

no straight line trajectories



causes everything to go into the origin
causes circular or elliptical motion about origin

Spiralling inward

Determining spiral:

$$\vec{X}' = \begin{bmatrix} -\frac{1}{2} & 1 \\ -1 & -\frac{1}{2} \end{bmatrix} \begin{bmatrix} 0 \\ 2 \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \end{bmatrix}$$

$$\vec{X}' = \begin{bmatrix} -\frac{1}{2} & 1 \\ -1 & -\frac{1}{2} \end{bmatrix} \begin{bmatrix} 2 \\ 0 \end{bmatrix} = \begin{bmatrix} -1 \\ -2 \end{bmatrix}$$

$$\vec{X}' = \begin{bmatrix} -\frac{1}{2} & 1 \\ -1 & -\frac{1}{2} \end{bmatrix} \begin{bmatrix} -2 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

May 13-9:50 AM