

$$\begin{array}{l} \sim \\ \sim \end{array} \Rightarrow \begin{array}{l} \sim \\ \sim \\ \hline 0=0 \end{array}$$

$$\begin{array}{l} \sim \\ \sim \end{array} \Rightarrow \begin{array}{l} \sim \\ \sim \\ \hline 0=23 \end{array} \rightarrow \text{No solution}$$

② Rref to solve systems in ②  
from class exercises:

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 7 \end{bmatrix}$$

$$\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array}$$

$$\begin{bmatrix} 1 & 2 & 4 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{array}{ccc} x & y & \text{no solution} \\ \begin{bmatrix} 1 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \\ 0x + 0y = 1 \end{array}$$

System from ① "ref's" to

$$\begin{matrix} & \overset{x}{1} & \overset{y}{-2} & \overset{z}{0} & 0 \\ \left[ \begin{array}{cccc} 1 & -2 & 0 & 0 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 0 \end{array} \right] \end{matrix}$$

$x - 2y = 0$   
 $x = 2y$

$x = 2t$   
 $y = t$   
 $z = 4$

$x, z$  are leading variables

$y$  is a free variable, call it  $t$ .  
 $y = t$

$$\begin{array}{cccccc}
 x_1 & x_2 & x_3 & x_4 & x_5 & \\
 \left[ \begin{array}{cccccc}
 1 & 3 & 0 & 0 & 7 & 1 \\
 0 & 0 & 1 & 0 & -5 & 2 \\
 0 & 0 & 0 & 1 & 2 & 3 \\
 0 & 0 & 0 & 0 & 0 & 0
 \end{array} \right]
 \end{array}$$

$$\rightarrow x_4 + 2x_5 = 3$$

$$x_4 = 3 - 2x_5 = 3 - 2t$$

leading:  $x_1, x_3, x_4$

free:  $x_2, x_5$

$$x_1 = 1 - 3s - 7t$$

$$x_2 = s$$

$$x_3 = 2 + 5t$$

$$x_4 = 3 - 2t$$

$$x_5 = t$$

Turn In: 1.4: 9, 13(b), 15

For each, give

$$2x + 3y = 7$$

$$x - 5y = 2$$

$$\begin{bmatrix} 2 & 3 & 7 \\ 1 & -5 & 2 \end{bmatrix}$$

\* system, any work getting it

\* augmented matrix

\* solution, with units if appropriate