

Consider $S = \left\{ \begin{bmatrix} a \\ b \\ a+b \end{bmatrix} \in \mathbb{R}^3 \right\}$

- a) Give a few vectors in S . $\begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}, \begin{bmatrix} 4 \\ 9 \\ 13 \end{bmatrix}, \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$
- b) Is S closed under addition?
- c) " " " " scalar multiplication?

$$\begin{bmatrix} a \\ b \\ a+b \end{bmatrix}, \begin{bmatrix} c \\ d \\ c+d \end{bmatrix} \in S$$

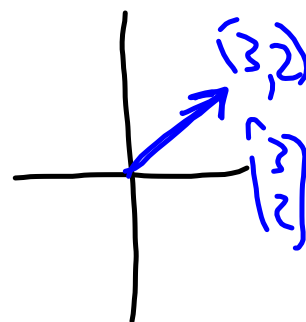
$$\begin{bmatrix} a \\ b \\ a+b \end{bmatrix} + \begin{bmatrix} c \\ d \\ c+d \end{bmatrix} = \begin{bmatrix} a+c \\ b+d \\ a+b+c+d \end{bmatrix} = \begin{bmatrix} a+c \\ b+d \\ (a+c)+(b+d) \end{bmatrix} \in S$$

Therefore S is closed under addition.

$$\Sigma_1 = \left\{ t \begin{bmatrix} 1 \\ -2 \end{bmatrix} \mid t \in \mathbb{R} \right\} = \left\{ \begin{bmatrix} 1 \\ -2 \end{bmatrix}, \begin{bmatrix} 3 \\ -6 \end{bmatrix}, \begin{bmatrix} -5 \\ 10 \end{bmatrix}, \dots \right\}$$

$t=1$ $t=3$ $t=-5$

$$\Sigma_1 = \left\{ \begin{bmatrix} 0 \\ 0 \end{bmatrix} + t \begin{bmatrix} 1 \\ -2 \end{bmatrix} \mid t \in \mathbb{R} \right\}$$



$$\begin{bmatrix} 3 \\ -6 \end{bmatrix} + \begin{bmatrix} -5 \\ 10 \end{bmatrix} = \begin{bmatrix} -2 \\ 4 \end{bmatrix} = -2 \begin{bmatrix} 1 \\ -2 \end{bmatrix} \in S_1$$

$$\begin{bmatrix} 1 \\ -2 \end{bmatrix} + \begin{bmatrix} 3 \\ -6 \end{bmatrix} = \begin{bmatrix} 4 \\ -8 \end{bmatrix} = 4 \begin{bmatrix} 1 \\ -2 \end{bmatrix} \in S_1$$

$$\pi \begin{bmatrix} -5 \\ 10 \end{bmatrix} = \begin{bmatrix} -5\pi \\ 10\pi \end{bmatrix} = -5\pi \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

$$S_2 = \left\{ \begin{bmatrix} 3 \\ 1 \end{bmatrix} + t \begin{bmatrix} 1 \\ -2 \end{bmatrix} \mid t \in \mathbb{R} \right\}$$
$$= \left\{ \begin{bmatrix} 5 \\ -3 \end{bmatrix}, \begin{bmatrix} 6 \\ -5 \end{bmatrix}, \begin{bmatrix} 7 \\ -7 \end{bmatrix}, \begin{bmatrix} 8 \\ -9 \end{bmatrix}, \dots \right\}$$

$$\begin{bmatrix} 13 \\ -12 \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \end{bmatrix} + \begin{bmatrix} 10 \\ -13 \end{bmatrix} \stackrel{?}{=} \cancel{\begin{bmatrix} 3 \\ 1 \end{bmatrix}} + \frac{10}{-2} \begin{bmatrix} 1 \\ -2 \end{bmatrix}$$

$$\sum_3^1 = \left\{ s \begin{bmatrix} 3 \\ 1 \end{bmatrix} + t \begin{bmatrix} 1 \\ -2 \end{bmatrix} \right\}$$

$$\begin{bmatrix} 248\pi \\ e-1 \end{bmatrix}$$

linear combination

$$\begin{bmatrix} \cdot \\ \cdot \\ \cdot \end{bmatrix} = s \begin{bmatrix} \cdot \\ \cdot \\ \cdot \end{bmatrix} + t \begin{bmatrix} \cdot \\ \cdot \\ \cdot \end{bmatrix}$$

$$s \begin{bmatrix} 3 \\ 1 \end{bmatrix} + t \begin{bmatrix} 1 \\ -2 \end{bmatrix} = \begin{bmatrix} 3 \\ -7 \end{bmatrix}$$

↑
years

$$s = -0.143$$

$$t = 3.43$$

