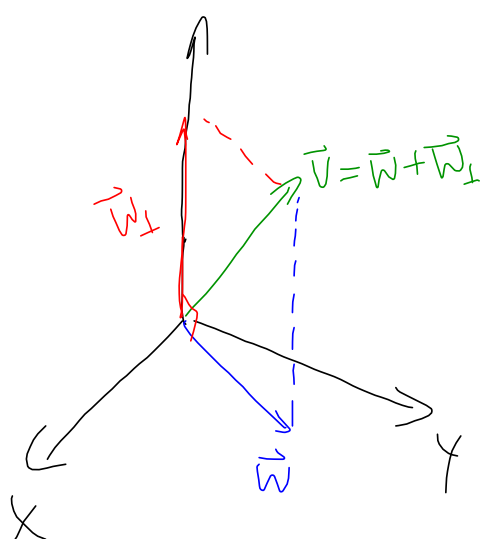


$W = \text{span} \left( \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} \right)$  is a subspace of  $\mathbb{R}^3$ .

What is it, geometrically? Give another vector in  $\mathbb{R}^3$  whose span is a subspace  $W^\perp$  for which every  $\vec{v} \in W^\perp$  is orthogonal to every  $\vec{u} \in W$ .



$$\begin{pmatrix} 5 \\ 3 \\ 0 \end{pmatrix}, \begin{pmatrix} -2 \\ 8 \\ 0 \end{pmatrix},$$

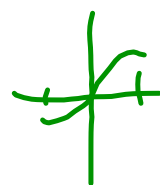
$$\begin{pmatrix} 9 \\ 5 \\ 0 \end{pmatrix}$$

$$W^\perp = \text{Span} \left( \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right)$$

$$C[-1,1] \quad \langle f, g \rangle = \int_{-1}^1 f(x)g(x) dx$$

$W = \mathcal{E}$  is even functions in here

$W^\perp =$  odd functions in  $C[-1,1]$ ?



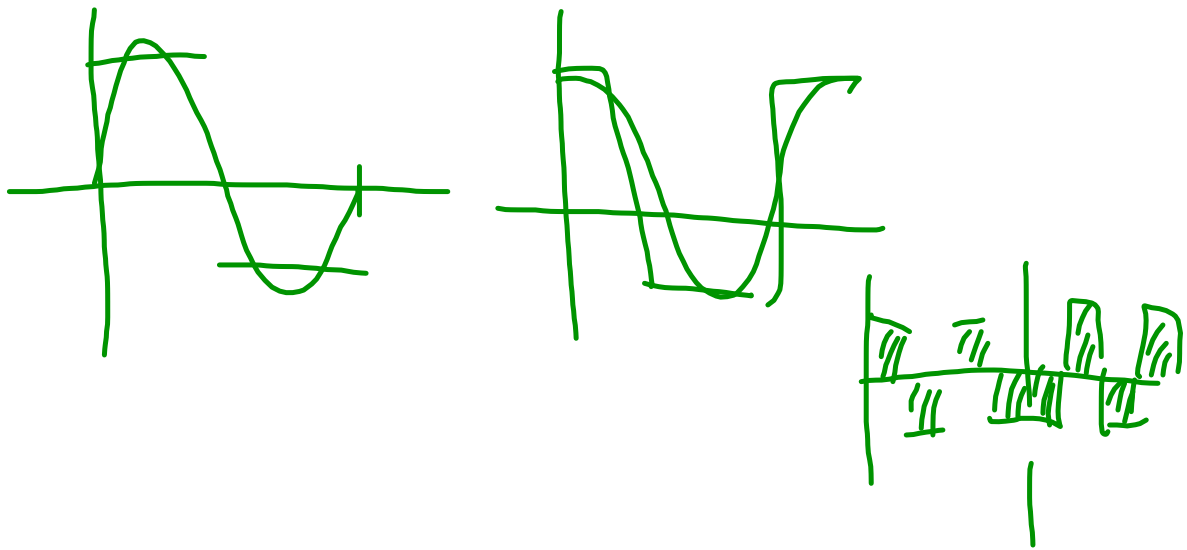
$\vec{v}, W, W^\perp$ 

$$\vec{v} = \vec{w} + \vec{w}_\perp = \text{proj}_W \vec{v} + \text{perp}_W \vec{v}$$
$$(\vec{v} - \text{proj}_W \vec{v})$$

$\mathbb{R}^5$  has basis  $\left\{ \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \dots \right\}$   
 $\vec{e}_1, \vec{e}_2$

$$W = \text{span}(\vec{e}_1, \vec{e}_2)$$

$$W^\perp = \text{span}(\vec{e}_3, \vec{e}_4, \vec{e}_5)$$



Due Monday:

Signal Processing 1: 4-9

3.3: 1,5

