

$$f(x) = x^2 + 3x - 2$$

Find and simplify the difference
quotient

$$\frac{f(x+h) - f(x)}{h}$$

$$\begin{aligned}
 f(x+h) &= (x+h)^2 + 3(x+h) - 2 \\
 &= (x+h)(x+h) + 3x + 3h - 2 \\
 &= x^2 + 2xh + h^2 + 3x + 3h - 2
 \end{aligned}$$

$$\frac{f(x+h) - f(x)}{h} = \frac{(x^2 + 2xh + h^2 + 3x + 3h - 2) - (x^2 + 3x - 2)}{h}$$

$$= \frac{x^2 + 2xh + h^2 + 3x + 3h - 2 - x^2 - 3x + 2}{h}$$

$$= \frac{2xh + h^2 + 3h}{h}$$

$$= \frac{h(2x + h + 3)}{h}$$

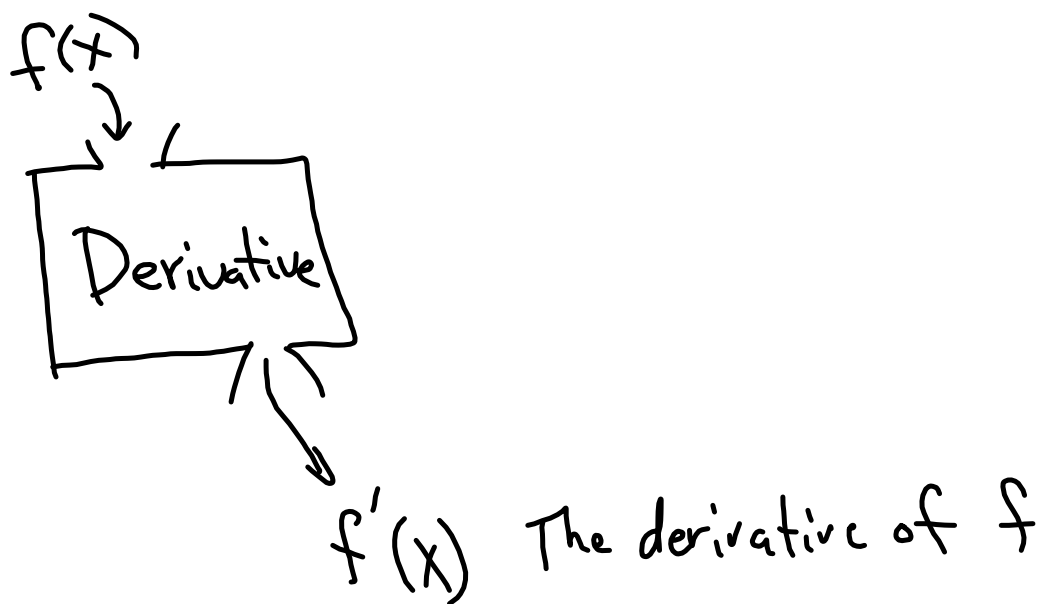
$$= 2x + h + 3$$

$$f(x) = 3x - 5$$

Find $\frac{f(x+h) - f(x)}{h}$

$$\begin{aligned} f(x+h) &= 3(x+h) - 5 \\ &= 3x + 3h - 5 \end{aligned}$$

$$\begin{aligned} \frac{f(x+h) - f(x)}{h} &= \frac{(3x + 3h - 5) - (3x - 5)}{h} \\ &= \frac{\cancel{3x} + 3h - 5 - \cancel{3x} + 5}{h} \\ &= \frac{3h}{h} \\ &= 3 \end{aligned}$$



Find the derivative of $x^0 = 1$

$$f(x) = 5x^3 - 7x^2 + 3x^1 - 2x^0$$

$$f'(x) = 3 \cdot 5x^{3-1} - 2 \cdot 7x^{2-1} + 1 \cdot 3x^{1-1} - 0 \cdot 2x^{0-1}$$

$$f'(x) = 15x^2 - 14x + 3.$$

$$g(x) = 4x^5 - 2x^4 + 7x^3 + x^2 + 6x - 1$$

$$g'(x) = 20x^4 - 8x^3 + 21x^2 + 2x + 6$$

g-prime

Differential

Integral

