

CB pg. 5: 1d)

$$\frac{1+2i}{3-4i} + \frac{2-i}{5i} = -\frac{2}{5}$$

$$\begin{aligned} \frac{1+2i}{3-4i} \left(\frac{3+4i}{3+4i} \right) + \frac{2-i}{5i} \left(\frac{5i}{5i} \right) &= \\ &= \frac{3+10i-8}{9+16} + \frac{10i+5}{-25} \\ &= \frac{-5+10i-(10i+5)}{25} \\ &= \frac{-5+10i-10i-5}{25} \\ &= \frac{-10}{25} \\ &= -\frac{2}{5} \end{aligned}$$

$$\overline{z + 3i} = \overline{z} + \overline{3i}$$

$$= z + \overline{3i}$$

$$= z - 3i$$

$$\overline{z_1 + z_2} = \overline{z_1} + \overline{z_2}$$

$$\overline{\overline{z}} = z$$

$$\overline{\overline{-z}} = -z$$

if z is imaginary

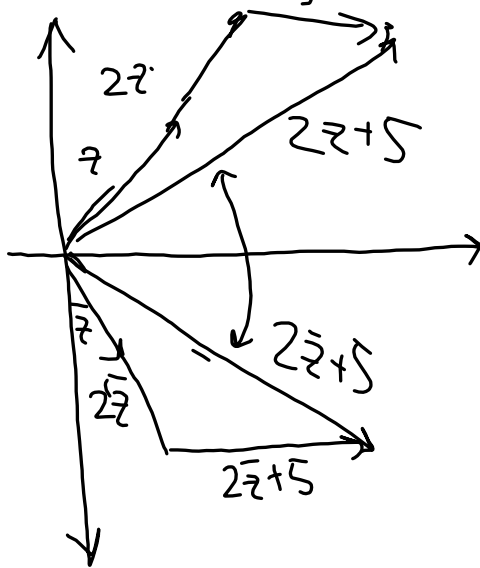
$$\overline{i z} = -i \bar{z}$$

$$\begin{aligned}\overline{i z} &= \overline{i} \bar{z} \\ &= -i \bar{z}\end{aligned}$$

$$\overline{z_1 z_2} = \bar{z}_1 \bar{z}_2$$

$$\overline{i} = -i$$

$$\begin{aligned}
 |(2\bar{z}+5)(\sqrt{2}-i)| &= |(2\bar{z}+5)| |(\sqrt{2}-i)| & (z_1 z_2) &= |z_1| |z_2| \\
 &= |(2\bar{z}+5)| (\sqrt{2^2+(-1)^2}) \\
 &= |(2\bar{z}+5)| (\sqrt{2+1}) & \text{Can skip to here} \\
 &= |(2\bar{z}+5)| (\sqrt{3})
 \end{aligned}$$



or $=\sqrt{3} |2\bar{z}+5|$

$$= \sqrt{3} |(2\bar{z}+5)|$$

$$\begin{aligned}
 |(2\bar{z}+5)(\sqrt{2}-i)| &= |(2\bar{z}+5)| |\sqrt{2}-i| \\
 &= \sqrt{3} |2\bar{z}+5| \\
 &= \sqrt{3} |\overline{2z+5}| \quad |\bar{\bar{z}}|=|z| \\
 &= \sqrt{3} |\overline{2z+5}| \quad \overline{z_1+z_2}=\bar{z}_1+\bar{z}_2 \\
 &= \sqrt{3} |\overline{2z}+\bar{5}| \quad \overline{z_1 z_2}=\bar{z}_1 \bar{z}_2 \\
 &= \sqrt{3} |2\bar{z}+5| \quad \bar{\bar{z}}=z \\
 & \quad \text{when } z \in \mathbb{R} \\
 &= \sqrt{3} |2z+5| \quad \bar{\bar{z}}=z
 \end{aligned}$$

z_1, z_2

Addition: $(2+3i) + (7-i) = 9+2i$

$$7e^{\frac{2\pi}{3}i} + \sqrt{4}e^{-\frac{\pi}{4}i} = ?$$

Multiplication: $7e^{\frac{2\pi}{3}i} \cdot \sqrt{4}e^{-\frac{\pi}{4}i} = 7\sqrt{4}e^{\frac{2\pi}{3}i - \frac{\pi}{4}i}$

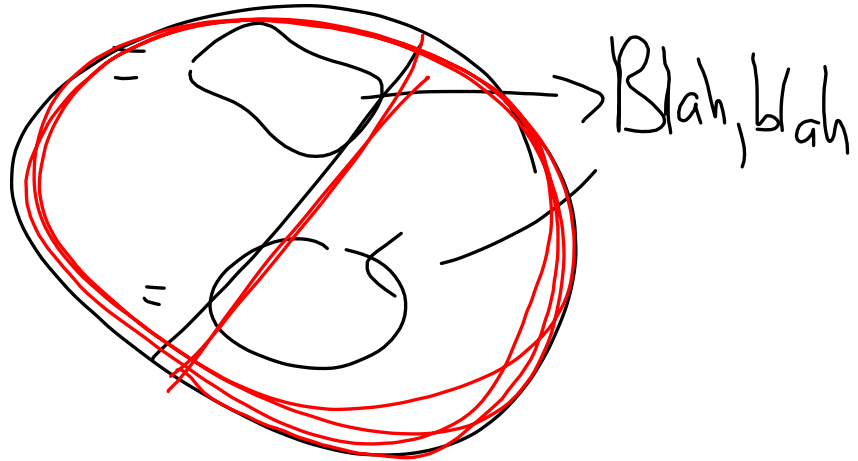
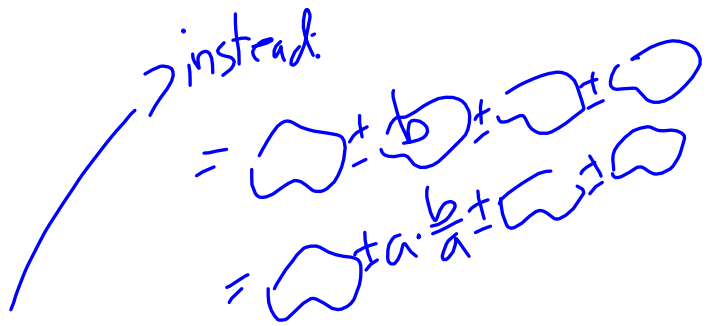
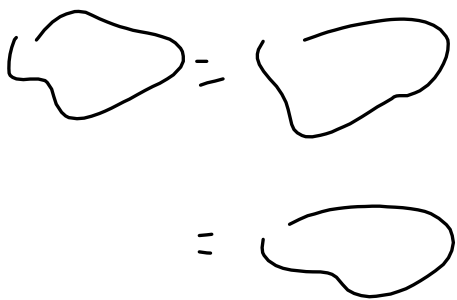
$$= 7\sqrt{4}e^{\left(\frac{2\pi}{3} - \frac{\pi}{4}\right)i}$$

$$\frac{ae^{bi}}{ce^{di}} = \frac{a}{c}e^{(b-d)i}$$

$$\sin(A+B)$$

$$e^{i\theta} = \cos\theta + i\sin\theta$$

Given $x + iy = a + ib$
 $\Rightarrow x = a, y = b$



Due Fri @ 3:00

EE: 10, 11

And show that

$$\frac{(\bar{z} - 3)(z + 3) - 2i}{|z|^2 + 6i \operatorname{Im} z - 9 + 2i}$$