

$$(-5i)^{\frac{1}{3}} = (5e^{(\frac{3\pi}{2} + 2\pi n)i})^{\frac{1}{3}}$$

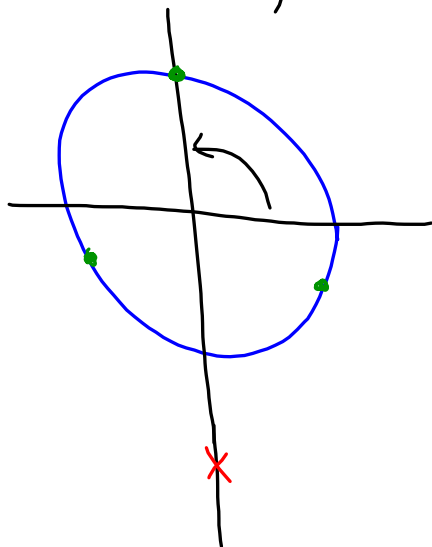
$$= \sqrt[3]{5} e^{(\frac{\pi}{2} + \frac{2\pi n}{3})i}$$

$$n=0: \sqrt[3]{5} e^{\frac{\pi}{2}}$$

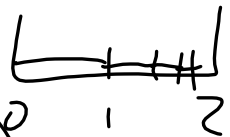
$$n=1: \sqrt[3]{5} e^{\frac{7\pi}{6}}$$

$$n=2: \sqrt[3]{5} e^{\frac{11\pi}{6}}$$

$$\sqrt[3]{5} i, \sqrt[3]{5} \left(-\frac{\sqrt{3}}{2} - \frac{1}{2}i\right),$$



$$1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} \dots$$

$$\frac{3}{5+2x} = \frac{3}{5} \left( 1 - \frac{2}{5}x + \frac{4}{25}x^2 - \dots \right)$$


$$r = -\frac{2}{5}x$$

$$5+2x=0$$

$$2x=-5$$

$$x=-\frac{5}{2}$$

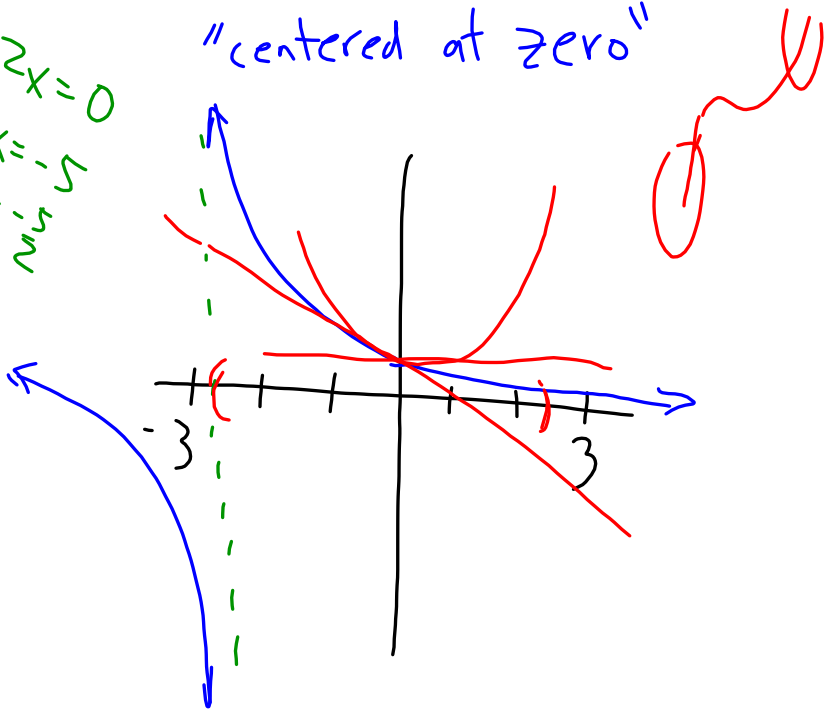
"centered at zero"

$$\left| -\frac{2}{5}x \right| < 1$$

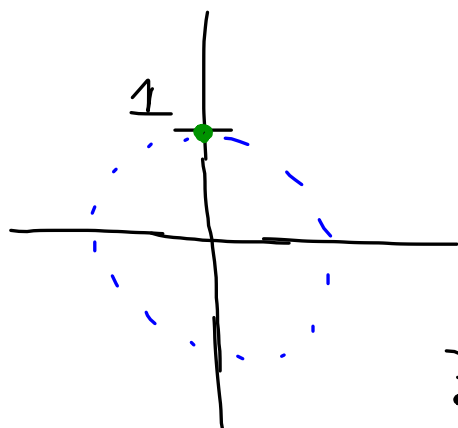
$$\left| -\frac{2}{5} \right| |x| < 1$$

$$\frac{2}{5} |x| < 1$$

$$|x| < \frac{5}{2}$$



$$i + z - \overset{-1z}{i z^2} - z^3 + z^4 - \dots = \frac{1}{z - i}$$



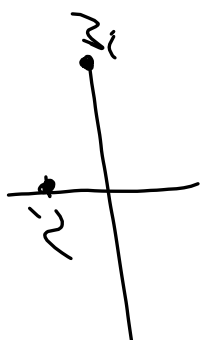
$$r = -iz$$

$$|-iz| < 1$$

$$|-i||z| < 1$$

$$|z| < 1$$

$$\frac{1}{(z+2)(z-3i)}$$



$$1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} +$$

$a_1 \quad a_2 \quad a_3 \quad a_4$

Calculate

$$S_1 = a_1$$

$$S_2 = a_1 + a_2$$

$$S_3 = a_1 + a_2 + a_3$$

$$S_1 = \frac{1}{1}$$

$$S_2 = \frac{3}{2}$$

$$S_3 = \frac{7}{4}$$

$$S_4 = \frac{15}{8}$$

If  $\lim_{n \rightarrow \infty} S_n$  exists, then that is what we

say the sum is.

$$S_n = \frac{2^n - 1}{2^{n-1}} = 2 - \frac{1}{2^{n-1}}$$

$|-|+|-|+|-|+$

$S_n$  like before

Define  $b_n = \frac{S_1 + S_2 + \dots + S_n}{n}$

Cesaro summation

Series converges to  $\frac{1}{2}$  in the Cesaro sense.

$n$	$a_n$	$S_n$	$b_n$
1	1	1	$\frac{1}{1} = 1$
2	-1	0	$\frac{1}{2} = \frac{1}{2}$
3	1	1	$\frac{2}{3}$
4	-1	0	$\frac{2}{4} = \frac{1}{2}$
5	1	1	$\frac{3}{5}$
6	-1	0	$\frac{2}{3}$
7	1	1	

