

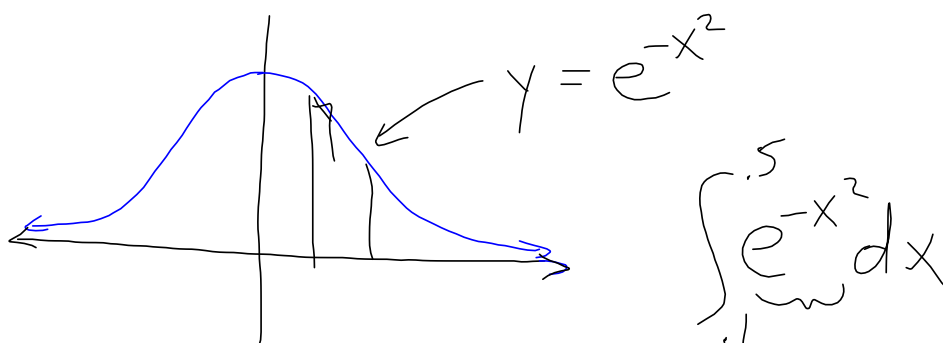
$$P(X > \frac{1}{2}) = \frac{7}{8}$$

$$P(X > \frac{1}{2}) = \int_{\frac{1}{2}}^{\infty} f(x) dx$$

$$f(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } 0 \leq x < 1 \\ 2-x & \text{if } 1 \leq x < 2 \\ 0 & \text{if } x \geq 2 \end{cases}$$

$$P(X = \frac{1}{2}) = \int_{\frac{1}{2}}^{\frac{1}{2}} x dx = 0$$

$$\begin{aligned} &= \int_{\frac{1}{2}}^1 x dx + \int_1^2 (2-x) dx \\ &= \left. \frac{1}{2} x^2 \right|_{\frac{1}{2}}^1 + \left[2x - \frac{1}{2} x^2 \right]_1^2 \\ &= \left(\frac{1}{2} - \frac{1}{8} \right) + \left[\underbrace{(4-2)}_{2 - \frac{3}{2}} - \left(2 - \frac{1}{2} \right) \right] = \frac{3}{8} + \frac{1}{2} = \frac{7}{8} \text{ (Hooray!)} \end{aligned}$$



$$S = \{1, 2, 3, 4, 5, 6\}$$

$$X(1) = 3 \quad \text{Ran}(X)$$

$$X(5) = 4$$

- ① finish assignment
- ② Work on Section 2.4

Discrete

$$\sum f(x)$$

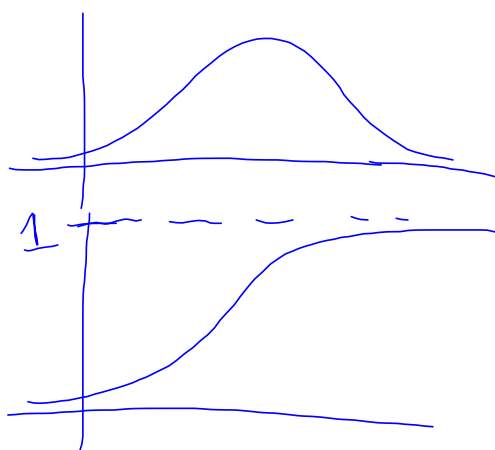
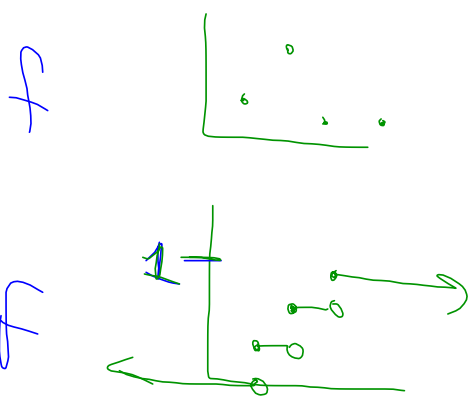
Continuous

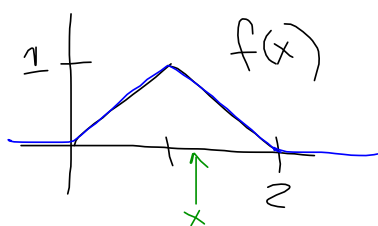
$$\int f(x) dx$$

$$\int_a^b f(x) dx = \lim \sum f(x) \Delta x$$

Discrete

Continuous





$$f(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & 0 \leq x < 1 \\ 2-x & 1 \leq x < 2 \\ 0 & x > 2 \end{cases}$$

F ?

$$F(x) = \int_{-\infty}^x f(t) dt$$

$$F(0) = 0 \quad F(2.1) = 1$$

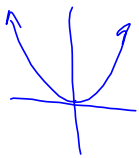
$$F(-1) = 0 \quad F(2) = 1$$

$$F(1) = \frac{1}{2}$$

for $0 \leq x < 1$, $F(x) = \int_0^x t dt = \frac{t^2}{2} \Big|_0^x = \frac{x^2}{2}$

for $1 < x \leq 2$, $F(x) = \int_{-\infty}^x f(t) dt = \int_0^1 t dt + \int_1^x (2-t) dt$

$$F(x) = \begin{cases} 0 & \text{if } x < 0 \\ \frac{1}{2}x^2 & \text{if } 0 \leq x < 1 \\ -\frac{1}{2}x^2 + 2x - 1 & \text{if } 1 \leq x < 2 \\ 1 & \text{if } x > 2 \end{cases}$$



$$= \frac{1}{2} + 2x - \frac{x^2}{2} - \frac{3}{2}$$

$$= -\frac{1}{2}x^2 + 2x - 1$$

